

GCSE - Mathematics

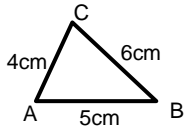
Topic: Sine and Cosine rules
- 2D and 3D

Tier: Higher

Grade: A*/ A



Starter. Which rule would you use?

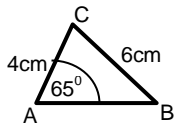
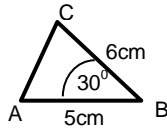


Find Angle ACB

Rule

Find length AC

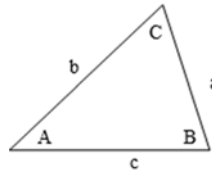
Rule



Find Angle ABC

Rule

Top Tips!



Use to find **side**

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

SINE RULE

To use the sine rule you must have
an angle and opposite side

Use to find **angle**

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

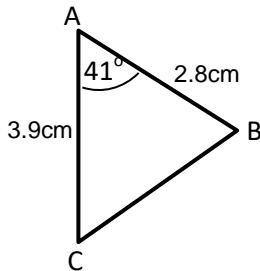
COSINE RULE

Use with questions were
Two sides and the **angle** between them
or all three sides is known

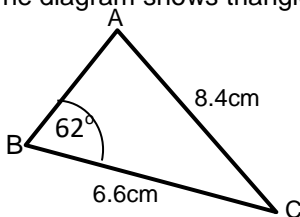
$$a^2 = b^2 + c^2 - 2bc \cos A$$

Skills:

Calculate the length of side BC



The diagram shows triangle ABC.

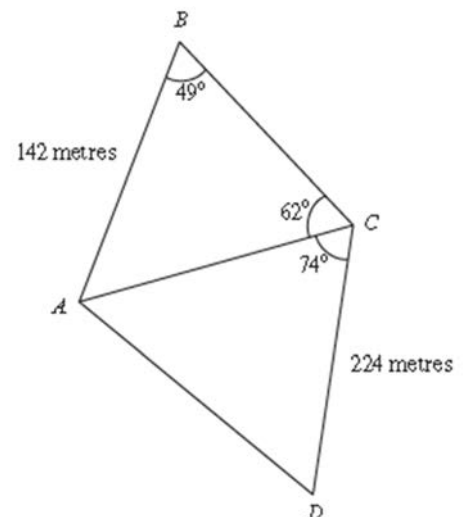


Calculate the size of the acute angle BAC

Examination Question:

2013 January Unitised U3 Higher Q16

A surveyor has recorded some measurements of a field on a sketch, as shown in the diagram.



The surveyor needs to know the length of the side AD in order to arrange for a drain to be installed. Calculate the length AD. [7]

Assessment for Learning

Video / QR code

GCSE - Mathematics

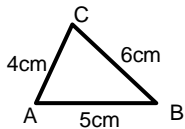
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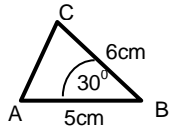
Starter. Which rule would you use?



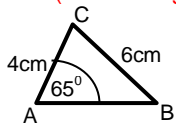
Find Angle ACB

Rule **Cosine Rule**
(3 sides)

Find length AC



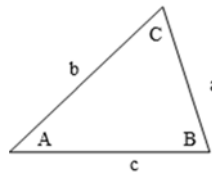
Rule **Cosine Rule**
(2 sides angle)



Find Angle ABC

Rule **Sine Rule**
(angle and opp side)

Top Tips!



Use to find **side**

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

SINE RULE

To use the sine rule you must have
an angle and opposite side

Use to find **angle**

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

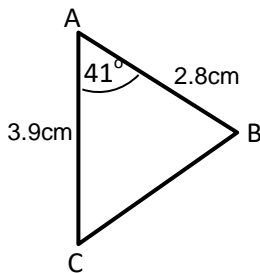
COSINE RULE

Use with questions were
Two sides and the **angle** between them *or all three sides* is known

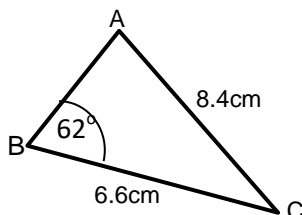
$$a^2 = b^2 + c^2 - 2bc \cos A$$

Skills:

Calculate the length of side BC



Cosine Rule $a^2 = b^2 + c^2 - 2bc \cos A$
 $a^2 = 3.9^2 + 2.8^2 - 2 \times 3.9 \times 2.8 \times \cos 41$
 $a^2 = 6.57$ $a = 2.6\text{cm}$



The diagram shows triangle ABC.
Calculate the size of the acute angle BAC

Sine Rule $\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$

$$\frac{\sin A}{6.6} = \frac{\sin 62}{8.4}$$

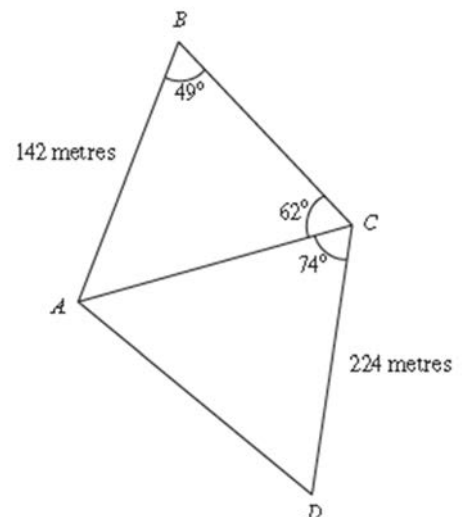
$$\sin A = \frac{\sin 62}{8.4} \times 6.6$$

$$\sin A = 0.6937 \quad A = 43.9^\circ$$

Examination Question:

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The surveyor needs to know the length of the side AD in order to arrange for a drain to be installed. Calculate the length AD. [7]

Length AC **Sine Rule** $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$
 $\frac{AC}{\sin 49} = \frac{142}{\sin 62}$ $AC = \frac{142}{\sin 62} \times \sin 49$
 $AC = 121.4\text{m}$

Length AD **Cosine Rule** $a^2 = b^2 + c^2 - 2bc \cos A$
 $a^2 = 121^2 + 224^2 - 2 \times 121 \times 224 \times \cos 74$
 $a^2 = 49875$
 $a = 223\text{m}$

Assessment for Learning

Video / QR code



